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A.R.C. Technical Report

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**Additional Data on Surface Slopes
of the RAE 100-104 Aerofoil Sections**

By

Edna M. Love and J. Williams

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FLUID MOTION SUB-COMMITTEEAERONAUTICAL RESEARCH COUNCILAdditional Data on Surface Slopes of the
RAE 100 - 104 Aerofoil Sections

- By -

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of the Aerodynamics Division, N.P.L.29th November, 1955SUMMARY

To supplement earlier data, the surface slopes of the RAE 100, 101 and 103 sections are tabulated, and for the RAE 102 and 104 sections additional values are quoted closer to the leading edge than before. An elementary but flexible method of specifying the minimum number of tangent planes needed for aerofoil manufacture is also given.

1. Introduction

Formulae and tables have already been published¹ for the accurate and rapid calculation of the surface slopes and curvatures of the RAE 100 - 104 aerofoil sections² and of more general 'rooftop-type' sections. In particular, the surface slopes of the RAE 102 and 104 shapes were tabulated¹ for application with a tangent-plane method of model manufacture³. Further data have since been evaluated for these shapes, and for the RAE 100, 101 and 103 sections.

2. Surface Slopes

It will be recalled that, forward of the wedge-shaped trailing edge, the ordinates of the RAE 100 - 104 shapes (unit chord) are given by the relation

$$y = a \{ f_0(x) + f_1(x) \} + cf_2(x) \quad \dots\dots(1)$$

where $x [= \frac{1}{2}(1 - \cos \theta)]$ denotes the chordwise distance behind the leading edge^{1,2}. The ratio of the constants a and c together with the position of maximum velocity $x = X_1$ prescribes the section shape, and for convenience the absolute values of the constants are usually assigned to give a section thickness of 10% chord. (see Table 5).

The values of dy/dx for the 10% thick 100, 101 and 103 sections are listed in Table 1a, and can be scaled linearly for other thickness-chord ratios. The corresponding auxiliary functions df_r/dx ($r = 0, 1$ and 2), which were needed for the evaluation of dy/dx for RAE 101 ($X_1 = 0.3$) and 103 ($X_1 = 0.5$),⁴ are tabulated in Table 2a. Additional data for RAE 102 ($X_1 = 0.4$) and 104 ($X_1 = 0.6$) at chordwise locations closer to the leading edge than before are also included in Tables 1b and 2b.

Values/

⁴The RAE 100 section ($X_1 = 0$) satisfies the simple equation

$$100 y = 14.8188 x^{\frac{1}{2}} (1-x)^{\frac{1}{2}} \begin{pmatrix} 8 \\ 1 - x \\ 9 \end{pmatrix}$$

forward of $x = 0.75$, where its wedge-shaped T.E. begins.

Values of certain transcendental functions needed for the calculation of df_r/dx at these additional points, and not published hitherto, are given in Tables 3a and 3b*. The aerofoil ordinates at these points are listed in Table 4, in the form of an extension to Table II of Ref.- 2.

3. Choice of Tangent Planes for Model Manufacture

For the manufacture of aerofoil models by tangent plane milling (or grinding)³, the tangent planes are usually selected so that the distance ℓ from the intersection of two neighbouring tangents to the required aerofoil profile (i.e., the excess metal) never exceeds a certain value, say 10^{-4} of the aerofoil chord.

A convenient approximate formula for this distance is

$$\ell \approx \left[1 + \left(\frac{\delta y}{\delta x} \right)^2 \right]^{\frac{1}{2}} \cdot \frac{\pi \delta \chi}{1440} \cdot \delta x \quad \dots\dots(2)$$

where the tangents to the profile at the adjacent points (x, y) and $(x + \delta x, y + \delta y)$ are at angles x and $x + \delta x$ degrees to the chord-line. This formula essentially assumes that the circular arc passing through these two points, and tangential to the aerofoil profile there, is a reasonable approximation to the profile between the points. Furthermore, except close to the leading edge where dy/dx and d^2y/dx^2 are not small, the relation (2) can for our purposes be simplified to

$$\ell \approx \left[1 + \frac{1}{2} \left(\frac{dy}{dx} \right)^2 \right] \cdot \frac{\pi \cdot \delta \chi}{1440} \cdot \delta x \quad \dots\dots(3)$$

The chordwise spacings δx , for a minimum number of tangent planes consistent with the limitation on ℓ , can be determined fairly simply by a trial and error method using the relations (2) and (3). For a chosen x and δx the values of dy/dx and $\delta \chi$ are readily derived from the tables of this report or Ref. 1. The trial and error procedure can be expedited by appealing to the relation (3), which shows for example that when the chordwise interval is doubled the value of ℓ is roughly quadrupled. Moreover, the value of ℓ is required only to an accuracy of about ± 10 percent in practice (e.g., to within 10^{-5} of the chord).

More elaborate procedures can be devised, but the above has so far proved reasonably quick and conveniently flexible.

References/

*These, with Table 3 of Ref. 1, facilitate the calculation of dy/dx and d^2y/dx^2 for a wider range of 'rooftop-type' sections.

References

| <u>No.</u> | <u>Author(s)</u> | <u>Title, etc.</u> |
|------------|-------------------------------------|---|
| 1 | J. Williams and Edna M. Love | Surface slopes and curvatures of the RAE 100 - 10 ₄ and other rooftop-type aerofoil sections. A.R.C. Current Paper 129. (October, 1952). |
| 2 | R. C. Pankhurst and H. B. Squire | Calculated pressure distributions for the RAE 100 - 10 ₄ aerofoil sections. R.A.E. T.N. Aero.2039. A.R.C. Current Paper 80. (March, 1950). |
| 3 | R. S. Marriner | The manufacture of aerofoil models by tangent plane milling. A.R.C. Current Paper 166. (June, 1953). |

TABLE 1a/

TABLE 1a

Surface Slopes for RAE 100, 101 and 103-Sections (10% Thick)

| x | RAE 100 | | RAE 101 | | RAE 103 | |
|--------|-----------------|--------------------|-----------------|--------------------|-----------------|--------------------|
| | $\frac{dy}{dx}$ | χ (degs.)* | $\frac{dy}{dx}$ | χ (degs.)* | $\frac{dy}{dx}$ | χ (degs.)* |
| 0 | ∞ | 90.000 | ∞ | 90.000 | ∞ | 90.000 |
| 0.0002 | 5.234871 | 79.185 | 4.366658 | 77.101 | 3.976417 | 75.884 |
| 0.0004 | 3.698526 | 74.870 | 3.086332 | 72.047 | 2.810694 | 70.415 |
| 0.0005 | 3.306682 | 73.174 | 2.759890 | 70.083 | 2.513488 | 68.305 |
| 0.0006 | 3.017314 | 71.664 | 2.518867 | 68.347 | 2.294059 | 66.447 |
| 0.0008 | 2.610889 | 69.043 | 2.180439 | 65.363 | 1.985965 | 63.273 |
| 0.001 | 2.333299 | 66.801 | 1.949382 | 62.843 | 1.775632 | 60.613 |
| 0.002 | 1.642996 | 58.673 | 1.375371 | 53.980 | 1.253194 | 51.411 |
| 0.003 | 1.335875 | 53.182 | 1.120491 | 48.252 | 1.021293 | 45.604 |
| 0.004 | 1.152033 | 49.041 | 0.968211 | 44.075 | 0.882788 | 41.438 |
| 0.005 | 1.026059 | 45.737 | 0.864057 | 40.829 | 0.788088 | 38.241 |
| 0.006 | 0.932691 | 43.005 | 0.787002 | 38.203 | 0.718050 | 35.680 |
| 0.007 | 0.859832 | 40.690 | 0.726980 | 36.016 | 0.663512 | 33.565 |
| 0.0075 | 0.828904 | 39.655 | 0.701535 | 35.051 | 0.640399 | 32.635 |
| 0.008 | 0.800868 | 38.690 | 0.678490 | 34.157 | 0.619467 | 31.777 |
| 0.009 | 0.751832 | 36.937 | 0.638234 | 32.547 | 0.582915 | 30.239 |
| 0.01 | 0.710186 | 35.382 | 0.604103 | 31.136 | 0.551934 | 28.896 |
| 0.012 | 0.642719 | 32.730 | 0.548944 | 28.764 | 0.501891 | 26.652 |
| 0.0125 | 0.628366 | 32.144 | 0.537234 | 28.246 | 0.491271 | 26.164 |
| 0.014 | 0.589876 | 30.535 | 0.505880 | 26.834 | 0.462848 | 24.837 |
| 0.016 | 0.546954 | 28.677 | 0.471009 | 25.221 | 0.431256 | 23.328 |
| 0.018 | 0.511131 | 27.073 | 0.441994 | 23.845 | 0.404986 | 22.047 |
| 0.02 | 0.480600 | 25.669 | 0.417335 | 22.652 | 0.382677 | 20.941 |
| 0.025 | 0.420268 | 22.795 | 0.368832 | 20.246 | 0.338850 | 18.719 |
| 0.03 | 0.374928 | 20.552 | 0.332610 | 18.398 | 0.306180 | 17.024 |
| 0.035 | 0.339073 | 18.730 | 0.304125 | 16.916 | 0.280538 | 15.671 |
| 0.04 | 0.309680 | 17.207 | 0.280891 | 15.690 | 0.259664 | 14.556 |
| 0.05 | 0.263663 | 14.771 | 0.244738 | 13.752 | 0.227276 | 12.804 |
| 0.06 | 0.228628 | 12.878 | 0.217387 | 12.265 | 0.202879 | 11.468 |
| 0.07 | 0.200594 | 11.343 | 0.195591 | 11.067 | 0.183524 | 10.399 |
| 0.075 | 0.188476 | 10.674 | 0.186185 | 10.547 | 0.175202 | 9.937 |
| 0.08 | 0.177366 | 10.058 | 0.177565 | 10.069 | 0.167593 | 9.514 |
| 0.09 | 0.157622 | 8.957 | 0.162237 | 9.215 | 0.154115 | 8.761 |
| 0.1 | 0.140504 | 7.998 | 0.148916 | 8.470 | 0.142465 | 8.108 |
| 0.12 | 0.111998 | 6.390 | 0.126562 | 7.213 | 0.123085 | 7.017 |
| 0.14 | 0.088907 | 5.081 | 0.108138 | 6.172 | 0.107324 | 6.126 |
| 0.15 | 0.078852 | 4.509 | 0.099966 | 5.709 | 0.100413 | 5.734 |
| 0.16 | 0.069597 | 3.981 | 0.092329 | 5.275 | 0.094009 | 5.371 |
| 0.18 | 0.053075 | 3.038 | 0.078324 | 4.479 | 0.082431 | 4.712 |
| 0.2 | 0.038694 | 2.216 | 0.065578 | 3.752 | 0.072128 | 4.125 |
| 0.22 | 0.026011 | 1.490 | 0.053689 | 3.073 | 0.062785 | 3.593 |
| 0.24 | 0.014712 | 0.843 | 0.042326 | 2.424 | 0.054175 | 3.101 |
| 0.25 | 0.009506 | 0.545 | 0.036740 | 2.104 | 0.050090 | 2.868 |
| 0.26 | 0.004565 | 0.262 | 0.031155 | 1.784 | 0.046128 | 2.641 |
| 0.28 | -0.004606 | -0.264 | 0.019712 | 1.129 | 0.038513 | 2.206 |
| 0.3 | -0.012935 | -0.741 | 0.006331 | 0.363 | 0.031222 | 1.788 |

TABLE 1a contd./

* $\chi = \tan^{-1} \frac{dy}{dx}$

TABLE 1a (Contd.)

| x | RAE 100 | | RAE 101 | | RAE 103 | |
|---------------------|-----------------|--------------------|-----------------|--------------------|-----------------|--------------------|
| | $\frac{dy}{dx}$ | χ (degs.)* | $\frac{dy}{dx}$ | χ (degs.)* | $\frac{dy}{dx}$ | χ (degs.)* |
| 0.32 | -0.020529 | -1.176 | -0.006549 | -0.375 | 0.024164 | 1.384 |
| 0.34 | -0.027473 | -1.574 | -0.016469 | -0.944 | 0.017258 | 0.989 |
| 0.35 | -0.030723 | -1.760 | -0.020896 | -1.197 | 0.013838 | 0.793 |
| 0.36 | -0.033836 | -1.938 | -0.025047 | -1.435 | 0.010427 | 0.597 |
| 0.38 | -0.039675 | -2.272 | -0.032657 | -1.870 | 0.003594 | 0.206 |
| 0.4 | -0.045037 | -2.579 | -0.039488 | -2.261 | -0.003327 | -0.191 |
| 0.42 | -0.049961 | -2.860 | -0.045660 | -2.614 | -0.010441 | -0.598 |
| 0.44 | -0.054479 | -3.118 | -0.051258 | -2.934 | -0.017888 | -1.025 |
| 0.45 | -0.056595 | -3.239 | -0.053861 | -3.083 | -0.021802 | -1.249 |
| 0.46 | -0.058620 | -3.355 | -0.056343 | -3.225 | -0.025894 | -1.483 |
| 0.48 | -0.062407 | -3.571 | -0.060963 | -3.489 | -0.034909 | -1.999 |
| 0.5 | -0.065861 | -3.768 | -0.065156 | -3.728 | -0.047009 | -2.691 |
| 0.52 | -0.068999 | -3.947 | -0.068952 | -3.944 | -0.058883 | -3.370 |
| 0.54 | -0.071835 | -4.109 | -0.072377 | -4.140 | -0.067219 | -3.846 |
| 0.55 | -0.073143 | -4.183 | -0.073957 | -4.230 | -0.070799 | -4.050 |
| 0.56 | -0.074381 | -4.254 | -0.075452 | -4.315 | -0.074086 | -4.237 |
| 0.58 | -0.076649 | -4.383 | -0.078193 | -4.471 | -0.079927 | -4.570 |
| 0.6 | -0.078647 | -4.497 | -0.080614 | -4.609 | -0.084953 | -4.856 |
| 0.62 | -0.080382 | -4.596 | -0.082726 | -4.729 | -0.089285 | -5.102 |
| 0.64 | -0.081860 | -4.680 | -0.084540 | -4.832 | -0.093006 | -5.314 |
| 0.65 | -0.082505 | -4.717 | -0.085338 | -4.878 | -0.094655 | -5.407 |
| 0.66 | -0.083086 | -4.750 | -0.086063 | -4.919 | -0.096170 | -5.493 |
| 0.68 | -0.084064 | -4.805 | -0.087300 | -4.989 | -0.098817 | -5.643 |
| 0.7 | -0.084796 | -4.847 | -0.088256 | -5.044 | -0.100977 | -5.766 |
| 0.72 | -0.085283 | -4.875 | -0.088933 | -5.082 | -0.102671 | -5.862 |
| 0.74 | -0.085526 | -4.888 | -0.089333 | -5.105 | -0.103915 | -5.933 |
| 0.75 | -0.085556 | -4.890 | -0.089430 | -5.110 | -0.104371 | -5.958 |
| 0.76 | | | -0.089459 | -5.112 | -0.104719 | -5.978 |
| 0.78 | | | | | -0.105090 | -5.999 |
| Wedge Tail | -0.085556 | -4.890 | -0.089429 | -5.110 | -0.104873 | -5.987 |
| At Inflection Point | -0.085556 | -4.890 | -0.089459 | -5.112 | -0.105119 | -6.001 |

* $\chi = \tan^{-1} \frac{dy}{dx}$

TABLE 1b/

TABLE 1b

Surface Slopes for RAE 102 and 104 Sections (10% Thick)

| x | RAE 102 | | RAE 104 | |
|--------|-----------------|--------------------|-----------------|--------------------|
| | $\frac{dy}{dx}$ | χ (degs.)* | $\frac{dy}{dx}$ | χ (degs.)* |
| 0.0002 | 4.139394 | 76.419 | 3.848090 | 75.433 |
| 0.0004 | 2.925811 | 71.130 | 2.720047 | 69.815 |
| 0.0005 | 2.616396 | 69.083 | 2.432454 | 67.652 |
| 0.0006 | 2.387949 | 67.278 | 2.220123 | 65.752 |
| 0.0008 | 2.067188 | 64.185 | 1.922002 | 62.512 |

Supplementary to Table 1 of Ref. 1

$$*\chi = \tan^{-1} \frac{dy}{dx}$$

TABLE 2a/

TABLE 2a

Values of Auxiliary Functions df_r/dx for $X_1 = 0.3$ and 0.5

| x | $X_1 = 0.3$ | | | $X_1 = 0.5$ | | |
|--------|------------------------|-----------------------|-----------------------|------------------------|-----------------------|-----------------------|
| | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ |
| 0 | ∞ | ∞ | ∞ | ∞ | ∞ | ∞ |
| 0.0002 | 15.894026 ₅ | 15.148453 | 4.302251 ₅ | 20.067154 ₅ | 12.861579 | 2.415998 ₅ |
| 0.0004 | 11.215488 ₅ | 10.726092 | 3.043416 ₅ | 14.171499 ₅ | 9.104507 | 1.708991 |
| 0.0005 | 10.021028 | 9.600197 | 2.722681 | 12.667272 | 8.147787 ₅ | 1.528846 ₅ |
| 0.0006 | 9.138404 | 8.769661 ₅ | 2.485973 | 11.556189 | 7.441956 ₅ | 1.395893 ₅ |
| 0.0008 | 7.897639 ₅ | 7.604997 ₅ | 2.153812 | 9.995146 | 6.451983 ₅ | 1.209319 ₅ |
| 0.001 | 7.049156 | 6.811275 | 1.927230 | 8.928478 ₅ | 5.777140 ₅ | 1.082042 ₅ |
| 0.002 | 4.932577 | 4.848594 ₅ | 1.365599 ₅ | 6.272931 | 4.107324 | 0.766516 |
| 0.003 | 3.985127 | 3.985115 ₅ | 1.117336 ₅ | 5.088837 ₅ | 3.371740 | 0.627001 |
| 0.004 | 3.414665 ₅ | 3.473848 ₅ | 0.969666 ₅ | 4.378531 | 2.935657 ₅ | 0.543992 |
| 0.005 | 3.021547 | 3.127263 | 0.869113 ₅ | 3.890791 ₅ | 2.639680 | 0.487452 ₅ |
| 0.006 | 2.728569 ₅ | 2.873108 | 0.795054 | 3.528556 | 2.422378 | 0.445797 ₅ |
| 0.007 | 2.498718 | 2.676867 | 0.737625 | 3.245326 | 2.254397 ₅ | 0.413486 ₅ |
| 0.0075 | 2.400755 ₅ | 2.594228 ₅ | 0.713363 | 3.124916 ₅ | 2.183597 ₅ | 0.399833 |
| 0.008 | 2.311721 | 2.519704 | 0.691438 | 3.015656 ₅ | 2.119714 | 0.387492 ₅ |
| 0.009 | 2.155416 | 2.390357 ₅ | 0.653269 ₅ | 2.824293 ₅ | 2.008745 ₅ | 0.366004 |
| 0.01 | 2.022001 | 2.281628 ₅ | 0.621055 ₅ | 2.661459 | 1.915364 ₅ | 0.347862 |
| 0.012 | 1.804332 | 2.108101 ₅ | 0.569348 ₅ | 2.396952 | 1.766102 ₅ | 0.318727 ₅ |
| 0.0125 | 1.757742 ₅ | 2.071663 | 0.558437 | 2.340547 ₅ | 1.734718 ₅ | 0.312576 ₅ |
| 0.014 | 1.632249 ₅ | 1.974900 ₅ | 0.529357 ₅ | 2.189030 ₅ | 1.651298 ₅ | 0.296178 ₅ |
| 0.016 | 1.491229 ₅ | 1.868826 ₅ | 0.497283 | 2.019556 ₅ | 1.559703 ₅ | 0.278079 ₅ |
| 0.018 | 1.372539 ₅ | 1.782001 | 0.470852 | 1.877641 | 1.484598 ₅ | 0.263153 |
| 0.02 | 1.270566 | 1.709395 ₅ | 0.4448610 | 1.756296 | 1.421693 ₅ | 0.250582 |
| 0.025 | 1.066500 ₅ | 1.570332 ₅ | 0.405602 | 1.515268 ₅ | 1.300929 ₅ | 0.226237 |
| 0.03 | 0.910526 ₅ | 1.470348 ₅ | 0.374314 | 1.332833 ₅ | 1.213873 | 0.208482 |
| 0.035 | 0.785344 | 1.394485 | 0.350573 ₅ | 1.187622 ₅ | 1.147721 ₅ | 0.194858 ₅ |
| 0.04 | 0.681400 | 1.334632 ₅ | 0.331395 ₅ | 1.067881 ₅ | 1.095522 ₅ | 0.184024 |
| 0.05 | 0.516149 ₅ | 1.245450 ₅ | 0.303141 | 0.878994 ₅ | 1.017941 | 0.167806 |
| 0.06 | 0.388346 ₅ | 1.181255 | 0.283132 ₅ | 0.733931 | 0.962588 ₅ | 0.156214 ₅ |
| 0.07 | 0.285084 ₅ | 1.131904 ₅ | 0.268313 ₅ | 0.617061 | 0.920714 | 0.147528 |
| 0.075 | 0.240279 ₅ | 1.110989 | 0.262300 | 0.566338 ₅ | 0.903267 | 0.143963 |
| 0.08 | 0.199170 ₅ | 1.091947 | 0.257023 ₅ | 0.519734 | 0.887598 ₅ | 0.140808 |
| 0.09 | 0.126216 | 1.058165 | 0.248275 | 0.436704 | 0.860455 ₅ | 0.135496 ₅ |
| 0.1 | 0.063364 ₅ | 1.028527 | 0.241442 | 0.364571 ₅ | 0.837524 | 0.131238 |
| 0.12 | -0.039288 ₅ | 0.976675 | 0.231982 ₅ | 0.244396 ₅ | 0.799974 ₅ | 0.124998 |
| 0.14 | -0.118730 | 0.929626 | 0.226606 ₅ | 0.147419 ₅ | 0.769177 ₅ | 0.120905 ₅ |
| 0.15 | -0.151566 ₅ | 0.906662 | 0.225101 | 0.105452 ₅ | 0.755288 ₅ | 0.119455 ₅ |
| 0.16 | -0.180455 ₅ | 0.883611 | 0.224270 ₅ | 0.067048 ₅ | 0.742047 ₅ | 0.118330 |
| 0.18 | -0.227691 | 0.836184 | 0.224433 ₅ | -0.000745 ₅ | 0.716766 ₅ | 0.116905 ₅ |
| 0.2 | -0.262326 ₅ | 0.785466 ₅ | 0.226860 | -0.058587 | 0.692174 | 0.116413 |
| 0.22 | -0.285323 ₅ | 0.729704 ₅ | 0.231545 ₅ | -0.108268 ₅ | 0.667477 | 0.116718 |
| 0.24 | -0.296817 | 0.666868 | 0.238730 | -0.151056 ₅ | 0.642093 ₅ | 0.117744 |
| 0.25 | -0.298020 ₅ | 0.631940 | 0.243431 | -0.170161 ₅ | 0.628998 ₅ | 0.118513 ₅ |
| 0.26 | -0.295879 ₅ | 0.593996 | 0.249036 ₅ | -0.187866 | 0.615567 | 0.119451 ₅ |
| 0.28 | -0.279330 ₅ | 0.505311 ₅ | 0.263998 | -0.219368 | 0.587512 | 0.121835 ₅ |
| 0.3 | -0.229416 | 0.374498 | 0.291353 ₅ | -0.246054 ₅ | 0.557574 ₅ | 0.124916 |

TABLE 2a (Contd.)

| x | $X_1 = 0.3$ | | | $X_1 = 0.5$ | | |
|--------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ |
| | | | | | | |
| 0.32 | -0.176009 | 0.243479 | 0.318402 | -0.268277 | 0.525406 | 0.128742 ₅ |
| 0.34 | -0.148898 | 0.154206 ₅ | 0.332452 | -0.286272 ₅ | 0.490638 | 0.133391 ₄₅ |
| 0.35 | -0.138753 | 0.115853 | 0.337385 | -0.293731 | 0.472151 | 0.136065 ₅ |
| 0.36 | -0.130075 ₅ | 0.080465 | 0.341277 | -0.300175 ₅ | 0.452851 | 0.138991 |
| 0.38 | -0.115908 ₅ | 0.016659 ₅ | 0.346174 ₅ | -0.310017 | 0.411540 | 0.145702 ₅ |
| 0.4 | -0.104769 | -0.039874 | 0.348767 | -0.315709 | 0.366056 | 0.153777 |
| 0.42 | -0.095757 | -0.090707 | 0.348552 | -0.317006 ₅ | 0.315510 | 0.163585 |
| 0.44 | -0.088316 ₅ | -0.136877 ₅ | 0.346067 | -0.313418 | 0.258575 ₅ | 0.175716 ₅ |
| 0.45 | -0.085066 | -0.158452 | 0.344022 | -0.309520 | 0.227075 ₅ | 0.182948 ₅ |
| 0.46 | -0.082080 | -0.179121 ₅ | 0.341458 ₅ | -0.303974 ₅ | 0.193019 | 0.191213 |
| 0.48 | -0.076792 ₅ | -0.217987 ₅ | 0.334812 | -0.286461 ₅ | 0.114156 | 0.212337 ₅ |
| 0.5 | -0.072268 ₅ | -0.253902 | 0.326170 ₅ | -0.250000 | 0 | 0.250000 |
| 0.52 | -0.068372 | -0.287205 ₅ | 0.315545 | -0.212337 ₅ | -0.114156 | 0.286461 ₅ |
| 0.54 | -0.064999 | -0.318176 ₅ | 0.302918 | -0.191213 | -0.193019 | 0.303974 ₅ |
| 0.55 | -0.063484 ₅ | -0.332861 | 0.295840 ₅ | -0.182948 ₅ | -0.227075 ₅ | 0.309520 |
| 0.56 | -0.062070 | -0.347048 ₅ | 0.288245 | -0.175716 ₅ | -0.258575 ₅ | 0.313418 |
| 0.58 | -0.059523 ₅ | -0.374023 | 0.271458 ₅ | -0.163585 | -0.315510 | 0.317006 ₅ |
| 0.6 | -0.057311 ₅ | -0.399276 ₅ | 0.252463 ₅ | -0.153777 | -0.366056 | 0.315709 |
| 0.62 | -0.055395 ₅ | -0.422967 ₅ | 0.231137 | -0.145702 ₅ | -0.411540 | 0.310017 |
| 0.64 | -0.053746 ₅ | -0.445243 | 0.207323 | -0.138991 | -0.452851 | 0.300175 ₅ |
| 0.65 | -0.053015 | -0.455894 ₅ | 0.194424 | -0.136065 ₅ | -0.472151 | 0.293731 |
| 0.66 | -0.052342 ₅ | -0.466244 ₅ | 0.180827 | -0.133394 ₅ | -0.490638 | 0.286272 ₅ |
| 0.68 | -0.051167 ₅ | -0.486111 ₅ | 0.151407 | -0.128742 ₅ | -0.525406 | 0.268277 |
| 0.7 | -0.050211 | -0.504989 | 0.118764 | -0.124916 | -0.557574 ₅ | 0.246054 ₅ |
| 0.72 | -0.049468 ₅ | -0.523032 ₅ | 0.082522 | -0.121835 ₅ | -0.587512 | 0.219368 |
| 0.74 | -0.048941 ₅ | -0.540419 ₅ | 0.042208 | -0.119451 ₅ | -0.615567 | 0.187866 |
| 0.75 | -0.048761 | -0.548931 | 0.020341 ₅ | -0.118513 ₅ | -0.628998 ₅ | 0.170161 ₅ |
| 0.76 | -0.048638 | -0.557360 ₅ | -0.002782 | -0.117744 | -0.642093 ₅ | 0.151056 ₅ |
| 0.78 | -0.048574 | -0.574118 | -0.053234 ₅ | -0.116718 | -0.667477 | 0.108268 ₅ |
| 0.8 | -0.048777 | -0.591033 | -0.110190 | -0.116413 | -0.692174 | 0.058587 |
| 0.82 | -0.049289 ₅ | -0.608570 ₅ | -0.175066 ₅ | -0.116905 ₅ | -0.716766 ₅ | 0.000745 ₅ |
| 0.84 | -0.050177 | -0.627395 | -0.249854 | -0.118330 | -0.742047 ₅ | -0.067048 ₅ |
| 0.85 | -0.050791 ₅ | -0.637583 | -0.291821 ₅ | -0.119455 ₅ | -0.755288 ₅ | -0.105452 ₅ |
| 0.86 | -0.051542 | -0.648503 ₅ | -0.337457 | -0.120905 ₅ | -0.769177 ₅ | -0.147419 ₅ |
| 0.88 | -0.053549 | -0.672480 ₅ | -0.442340 | -0.124998 | -0.799974 ₅ | -0.244396 ₅ |
| 0.9 | -0.056480 | -0.705028 ₅ | -0.571824 ₅ | -0.131238 | -0.837524 | -0.364571 ₅ |
| 0.92 | -0.060858 | -0.748213 ₅ | -0.739069 | -0.140808 | -0.887598 ₅ | -0.519734 |
| 0.925 | -0.062285 | -0.761874 | -0.789410 | -0.143963 | -0.903267 | -0.566338 ₅ |
| 0.94 | -0.067786 ₅ | -0.813889 ₅ | -0.971058 ₅ | -0.156214 ₅ | -0.962588 ₅ | -0.733931 |
| 0.95 | -0.072955 | -0.862602 | -1.129184 ₅ | -0.167806 | -1.017941 | -0.878994 ₅ |
| 0.96 | -0.080153 | -0.930903 | -1.336371 ₅ | -0.184024 | -1.095522 ₅ | -1.067881 ₅ |
| 0.975 | -0.098801 | -1.111286 ₅ | -1.832347 ₅ | -0.226237 | -1.300929 ₅ | -1.515268 ₅ |
| 0.98 | -0.109527 | -1.217002 ₅ | -2.102042 | -0.250582 | -1.421693 ₅ | -1.756296 |
| 0.9875 | -0.136797 | -1.490199 | -2.760847 | -0.312576 ₅ | -1.734718 ₅ | -2.340547 ₅ |
| 1.0 | -∞ | -∞ | -∞ | -∞ | -∞ | -∞ |

TABLE 2b/

TABLE 2b

Values of Auxiliary Functions df_r/dx for $X_1 = 0.4$ and 0.6

| x | $X_1 = 0.4$ | | | $X_1 = 0.6$ | | |
|--------|-----------------------|------------------------|-----------------------|------------------------|-----------------------|-----------------------|
| | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ | $\frac{df_0}{dx}$ | $\frac{df_1}{dx}$ | $\frac{df_2}{dx}$ |
| 0.0002 | 18.155662 | 13.903803 ₅ | 3.285266 | 21.718070 ₅ | 11.949683 | 1.676978 |
| 0.0004 | 12.817784 | 9.843281 ₅ | 2.523931 ₅ | 15.340399 | 8.458385 | 1.186213 ₅ |
| 0.0005 | 11.455540 | 8.809377 | 2.078989 | 13.713449 ₅ | 7.569291 | 1.061165 ₅ |
| 0.0006 | 10.449183 | 8.046640 | 1.898215 ₅ | 12.511836 | 6.913328 | 0.968875 |
| 0.0008 | 9.034978 ₅ | 6.976932 | 1.644538 ₅ | 10.823837 ₅ | 5.993250 ₅ | 0.839361 |

Supplementary to Table 2 of Ref. 1

TABLE 3a

Values of Transcendental Functions for the Determination of df_r/dx and d^2f_r/dx^2

| x | cos θ | sin θ | cosec θ | cot θ | cosec ³ θ |
|--------|--------------|-----------------------|----------------|--------------|-----------------------------|
| 0.0002 | 0.9996 | 0.028281 ₄ | 35.358875 | 35.344732 | 44207.435 |
| 0.0004 | 0.9992 | 0.0399920 | 25.005002 | 24.984997 | 15634.380 |
| 0.0005 | 0.999 | 0.0447102 | 22.366272 | 22.343906 | 11188.730 |
| 0.0006 | 0.9988 | 0.0489751 | 20.418541 | 20.394039 | 8512.8331 |
| 0.0008 | 0.9984 | 0.0565459 | 17.684745 | 17.656449 | 5530.9075 |

Supplementary to Table 3a of Ref. 1

TABLE 3b

Values of $\frac{1}{\pi} \log_e \frac{\sin \frac{1}{2} |\theta - \theta_1|}{\sin \frac{1}{2} (\theta + \theta_1)}$

| x | X_1 θ_1 | 0.3 | 0.4 | 0.5 | 0.6 |
|--------|---------------------|-----------|-----------|-----------|-----------|
| | | 1.1592795 | 1.3694384 | 1.5707963 | 1.7721542 |
| 0.0002 | | 0.0137561 | 0.0110288 | 0.0090047 | 0.0073521 |
| 0.0004 | | 0.0194590 | 0.0156002 | 0.0127366 | 0.0103990 |
| 0.0005 | | 0.0217586 | 0.0174433 | 0.0142412 | 0.0116272 |
| 0.0006 | | 0.0238384 | 0.0191101 | 0.0156017 | 0.0127379 |
| 0.0008 | | 0.0275333 | 0.0220708 | 0.0180185 | 0.0147106 |

Supplementary to Table 3b of Ref. 1.

TABLE 4/

TABLE 4

Co-ordinates of RAE 100 - 104 (10% Thick)

| x | 100 y | | | | |
|--------|---------|---------|---------|---------|---------|
| | RAE 100 | RAE 101 | RAE 102 | RAE 103 | RAE 104 |
| 0.0002 | 0.2095 | 0.1747 | 0.1656 | 0.1591 | 0.1540 |
| 0.0004 | 0.2962 | 0.2471 | 0.2342 | 0.2250 | 0.2177 |
| 0.0005 | 0.3311 | 0.2762 | 0.2618 | 0.2515 | 0.2434 |
| 0.0006 | 0.3627 | 0.3025 | 0.2868 | 0.2755 | 0.2666 |
| 0.0008 | 0.4187 | 0.3493 | 0.3311 | 0.3181 | 0.3078 |

Supplementary to Table II of Ref. 2

TABLE 5

Basic Design Constants for RAE 100 - 104 Sections

| Aerofoil | RAE 100 | 101 | 102 | 103 | 104 |
|----------|-----------|-----------|-----------|-----------|-----------|
| X_1 | 0 | 0.3 | 0.4 | 0.5 | 0.6 |
| a = b | 0.214049 | 0.147860 | 0.134822 | 0.125357 | 0.117920 |
| c | -0.049396 | -0.051899 | -0.055681 | -0.062678 | -0.072757 |

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